

Math 1220, Problem Set #1

Name:

Due: Friday, January 21st. *Show all work for partial credit! (No work, no credit).*

1. Use  $u$ -substitution to find the following indefinite integrals:

(a)  $\int 6y\sqrt{4+y^2}dy$

(b)  $\int \frac{x}{x^2+4}dx$

2. Compute the value of the following definite integrals:

(a)  $\int_0^{\pi/3} \frac{\tan z}{\cos^2 z} dz$

(b)  $\int_1^4 \left(2x + \frac{1}{x}\right) dx$

3. Find the area of the region in the first quadrant bounded by the curves  $y = 4 - x^2$  and  $y = 2 - x$ .

4. Integrate with respect to  $y$  to find the area of the region bounded by  $y = x^3$ ,  $x = 0$ , and  $y = 8$ .

5. Compute the volume of the solid generated by revolving the region under the curve  $y = \sqrt{x} + 1$  for  $x$  in  $[0, 4]$  around the  $x$ -axis.